

# Towards a Common Mobility Metric for Comparative Studies of Mobile Ad Hoc Networks: Results and Challenges

Xavier Pérez-Costa  
UPC Barcelona, Spain and NEC Europe Ltd.  
xavier.perez-costa@ccrle.nec.de

Christian Bettstetter  
TU Munich, Germany  
bettstetter@ei.tum.de

Hannes Hartenstein  
NEC Europe Ltd.  
hannes.hartenstein@ccrle.nec.de

## The Need for Mobility Models and Metrics

- The performance of a mobile ad hoc network depends on its ability to adapt to changes in network topology due to the nodes' mobility.
- Mobility models: key element for mobile ad hoc network simulation since changes in network topology depend on them.
- Mobility metrics: needed to assess the degree of dynamicity of a scenario *independently* of the mobility model used.
  - A mobility metric should provide a quantitative measure of mobility that is *relevant* to assess performance of the network.
  - Today: tuning parameters of a specific mobility model are used that do not provide an accurate measure of mobility, e.g., 'speed' or 'pause time'.

## Topological Change Rate (TCR) as a Mobility Metric

- TCR is the 'natural' mobility metric: reflects changes in network topology perfectly and is independent of specific tuning parameters of the mobility model.
- Potentially allows *comparability* of results obtained with different mobility models and/or scenarios.
- There is already some related work in this direction [1]
- However, for most models the TCR cannot be directly configured. Instead, analytical derivations or a simulative assessment of the TCR are needed.

## Random Waypoint (RWP) Mobility: Basics and Recent Insights

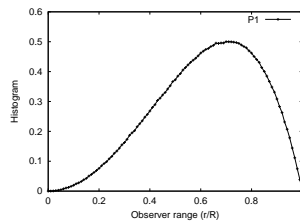
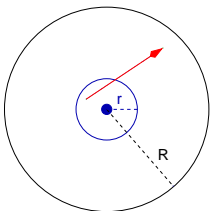
- Heavily used in ad hoc network simulations.
- A node selects the next waypoint by sampling from a uniform distribution over the system area; the node moves with constant or a speed sampled from a distribution to the waypoint; it might pause there and then iterates the scheme.
- But recent insights show some deficiencies:
  - RWP spatial node distribution non-uniform [2].
  - RWP speed distribution over time has intricacies [3].

## Topological change rate of RWP: Analytical results

- Consider one node following the RWP mobility model and one static observer in the center of a circular system area.
- Due to the *ergodicity* of the RWP process, each transition period – which is not independent of the next one other – can be treated as if they were independent (see [4]).
- We derived the TCR of the RWP model in 3 steps:

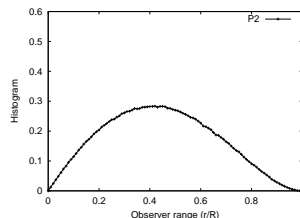
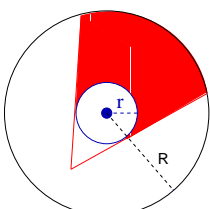
Step 1: Probability of *one* topological change in a transition:

$$P1 = 2 \cdot r_{00}^2 \cdot (1 - r_{00}^2) \text{ where } r_{00} = \frac{r}{R}$$



Step 2: Probability of *two* topological changes in a transition:

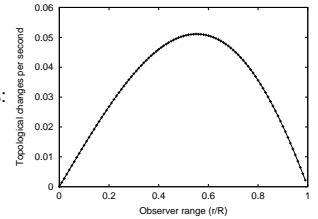
$$P2 = \frac{1}{2\pi} (\pi - 3 \cdot r_{00}^2 \cdot \pi + 2 \cdot \arcsin(r_{00}) + 4 \cdot r_{00} \cdot \sqrt{1 - r_{00}^2} - 2 \cdot r_{00}^2 \cdot \arcsin(r_{00}) - 4 \cdot r_{00}^3 \cdot \sqrt{1 - r_{00}^2} - 2 \cdot \arccos(r_{00}) + 2 \cdot r_{00}^4 \cdot \pi + 2 \cdot r_{00}^2 \cdot \arccos(r_{00}))$$



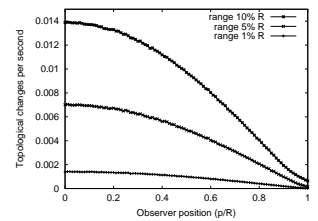
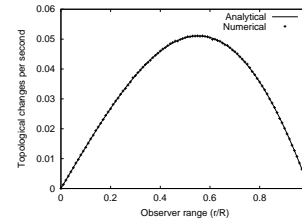
Step 3: Expected number of topological changes per time unit:

$$E_{top\_ch/s} = (P1 + 2 \cdot P2) \cdot \frac{E\{speed\}}{E\{mov\_length\}}$$

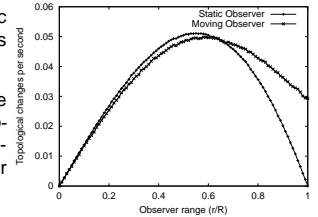
- $E\{mov\_length\} = \frac{128}{43\pi} \cdot R$  [4]
- Maximum topological change rate/s: 0.051 at  $r = 0.055 \cdot R$
- ...



## Topological Change Rate of RWP: Simulation Results



- The analytical expression for the static observer in the center case matches perfectly the simulation results
- The static observer in the center case yields the topological change rate *upper bound* compared to static observers located in different positions or moving observers



- The dependency of the topological change rate with respect to the speed of the mobile nodes or the number of mobile nodes is linear

## Contribution and Future steps

- Proposal of a mobility metric independent of the mobility model used and the considered scenario that allows performance comparison of results that depend on the mobility generated
- Analytical derivation and simulative evaluation of the topological change rate mobility metric.
- Enhance understanding of the Random Waypoint Mobility model.
- Propose a research agenda of what should be done *i)* to design a better mobility model and *ii)* to ... mobility metric.
- The upper bound for other mobility models should be obtained to make a comparative study of the performance under the same TCR conditions to validate the hypothesis of the TCR independence of the mobility model.

## References

- [1] B. Kwak, N. Song, and L.E. Miller, "A Mobility Measure for Mobile Ad-Hoc Networks," to appear in IEEE Communication Letters, 2003.
- [2] C. Bettstetter, "Smooth is Better than Sharp: A random mobility model for simulation of wireless networks," In Proceedings of ACM MSWIM, 2001.
- [3] J. Yoon, M. Liu, and B. Noble, "Random Waypoint Considered Harmful," In Proceedings of IEEE Infocom, 2003.
- [4] Chr. Bettstetter, H. Hartenstein, and X. Pérez-Costa, "Stochastic Properties of the Random Waypoint Mobility Model," to appear in ACM Kluwer Wireless Networks Special Issue on Modeling & Analysis of Mobile Networks, 2003.

